DSC 40B - Discussion 02

Problem 1.

- a) Let $f(n) = 12log_2(3^{n^2-2n} + 2^{logn} 10n^2 log_3n)$. Which of the following asymptotic bounds on f is true?
- **b**) What is the best case time complexity of the following function?

return False

Problem 2. $n^2 \pm 2n =$

$$f(n) = \frac{n^2 + 2n - 5}{n - 10}$$

Problem 3.

Consider the algorithm below.

```
def bogosearch(numbers, target):
"""search by randomly guessing. `numbers` is an array of n numbers"""
n = len(numbers)
while True:
    # randomly choose a number between 0 and n-1 in constant time
    guess = np.random.randint(n)
    if numbers[guess] == target:
        return guess
```

We will set up the analysis of the expected time complexity of this algorithm.

- a) What are the cases? How many are there?
- **b)** What is the probability of case α ?
- c) What is the running time in case α ?

Problem 4.

Provide a tight theoretical lower bound for the problems given below. Provide justification for your answer.

- a) Given an array of n numbers, find the sum of the numbers in the array.
- b) Given a sorted array of $n \ge 2$ numbers, find the second largest number in the array.

Problem 5.

Let $T_1(n) = \Theta(n^2)$, $T_2(n) = O(n^3)$, and $T_3(n) = \Omega(n^4)$ and $T_3(n) = O(n^4 \log n)$ each represent the runtime of different functions. What are the best bounds that can be placed on the following functions?

- **a)** $T_1(n) + T_2(n)$
- **b)** $T_1(n) \cdot T_3(n)$